

# Limit Cycle Suppression Technique Using Random Signal In Delta-Sigma DA Modulator

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## Objective

- **Development of high linear & high resolution  $\Delta\Sigma$  DAC**

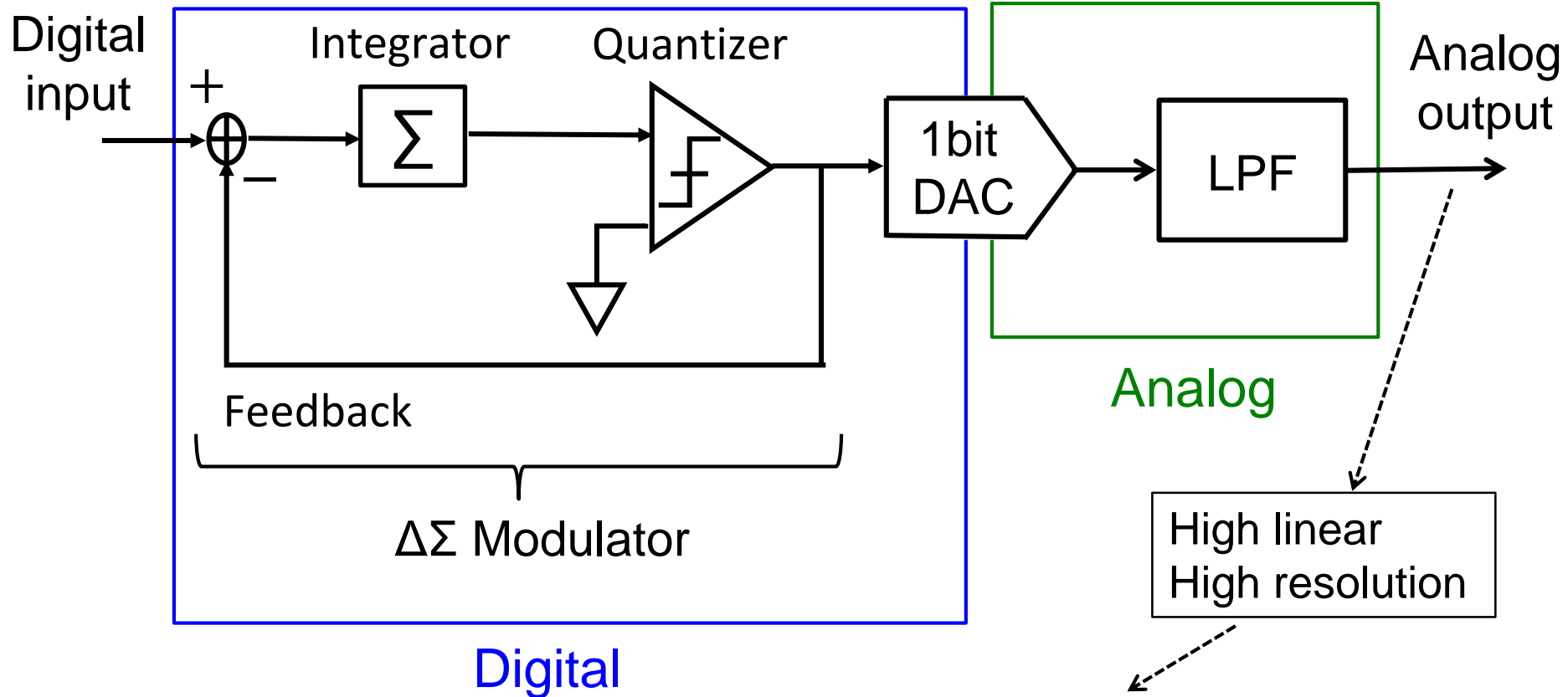
## Studies

- **Limit cycle suppression using random signal at quantizer input.**

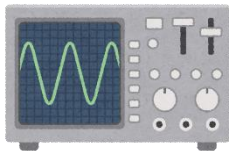
- Research Background
- Proposed Circuit
- Simulation Configuration & Results
- Conclusion

- **Research Background**
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# $\Delta\Sigma$ DA Converter



< Usage >

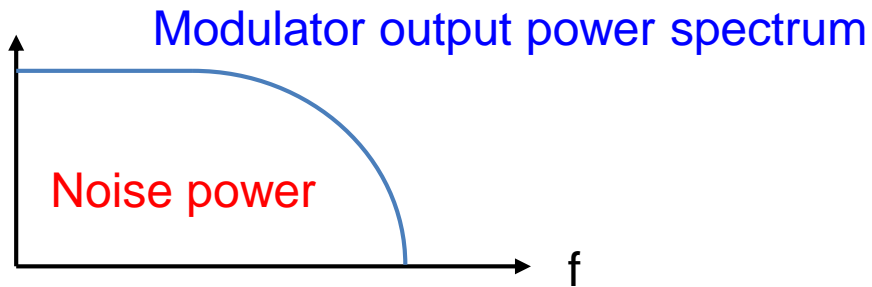


- Measurement
- Audio system
- Satellite communication

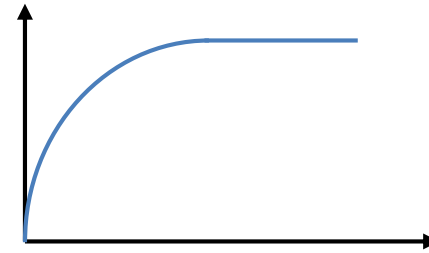


# Modulator type

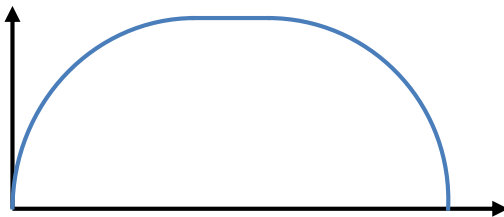
(1) low-pass (LP) type



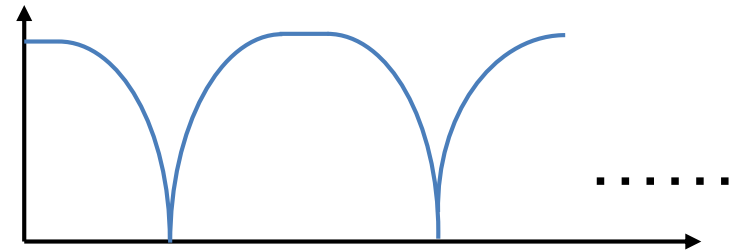
(2) high-pass (HP) type



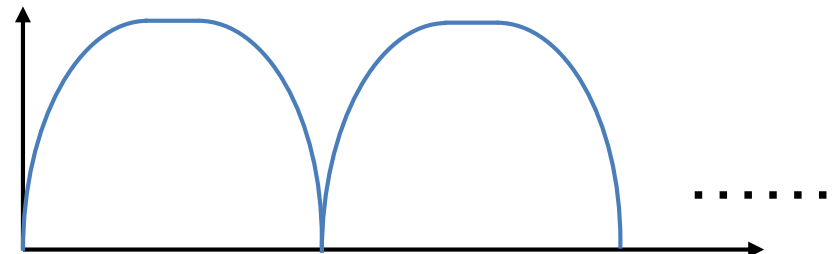
(3) band-pass (BP) type



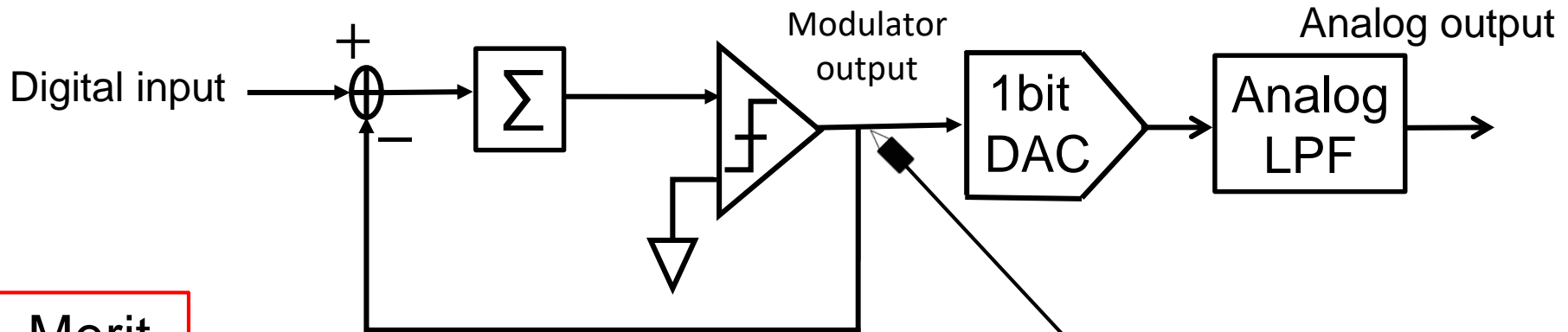
(4) multi-BP type I



(5) multi-BP type II



# Merits & Demerits of $\Delta\Sigma$ DAC



## Merit

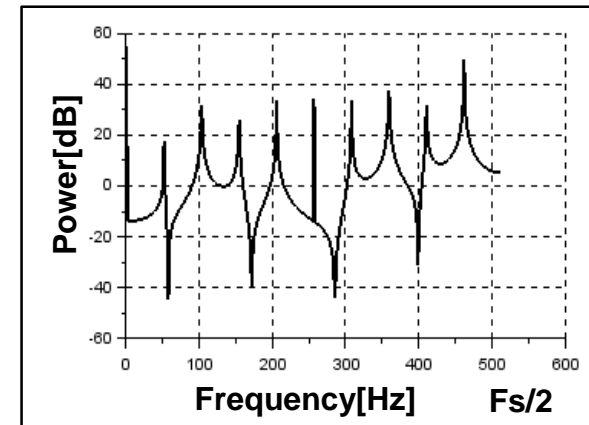
- Mostly digital circuit
- High linear & high resolution for low frequency signal generation

## Demerit

- Limit cycle problem for small input

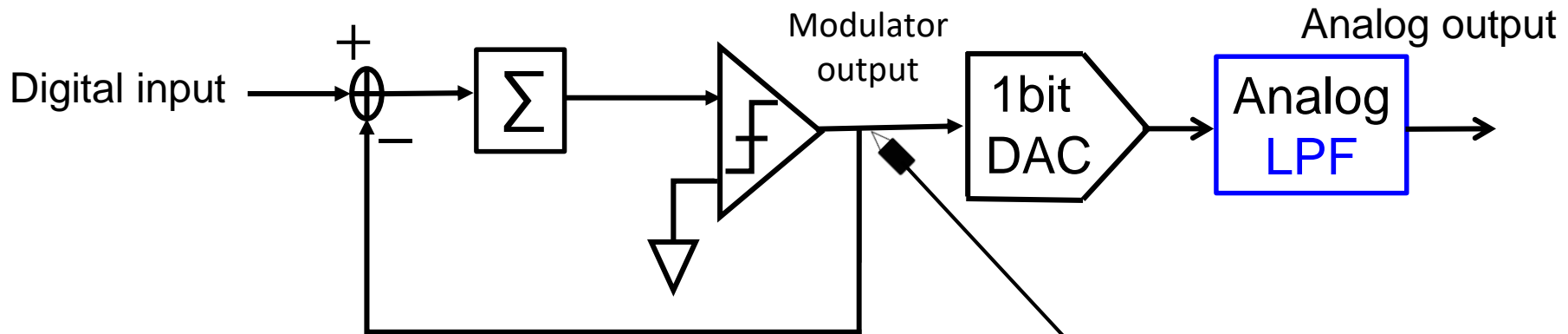


Limit cycle



✘ Due to modulator nonlinearity by quantizer

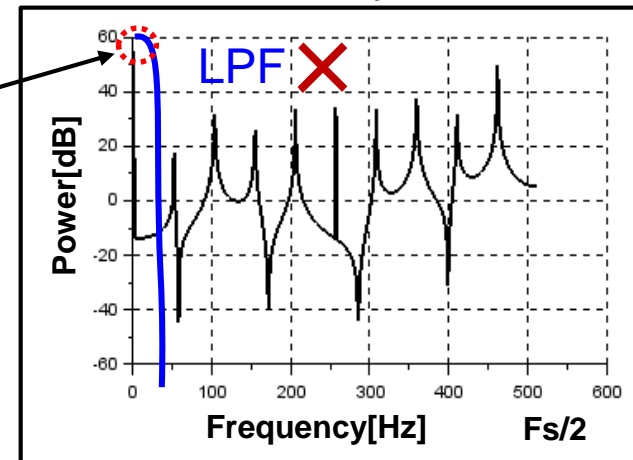
# Limit Cycle Problem



Removal of analog signal by LPF sharply

⇒ difficult

$$\text{Analog output} = \text{Signal} + \frac{\text{Limit cycle}}{\text{(Noise)}}$$

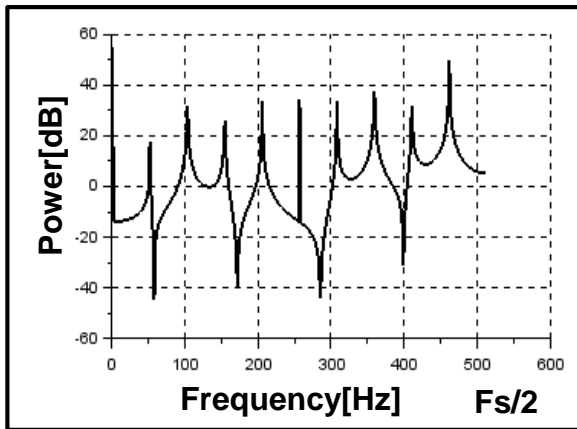
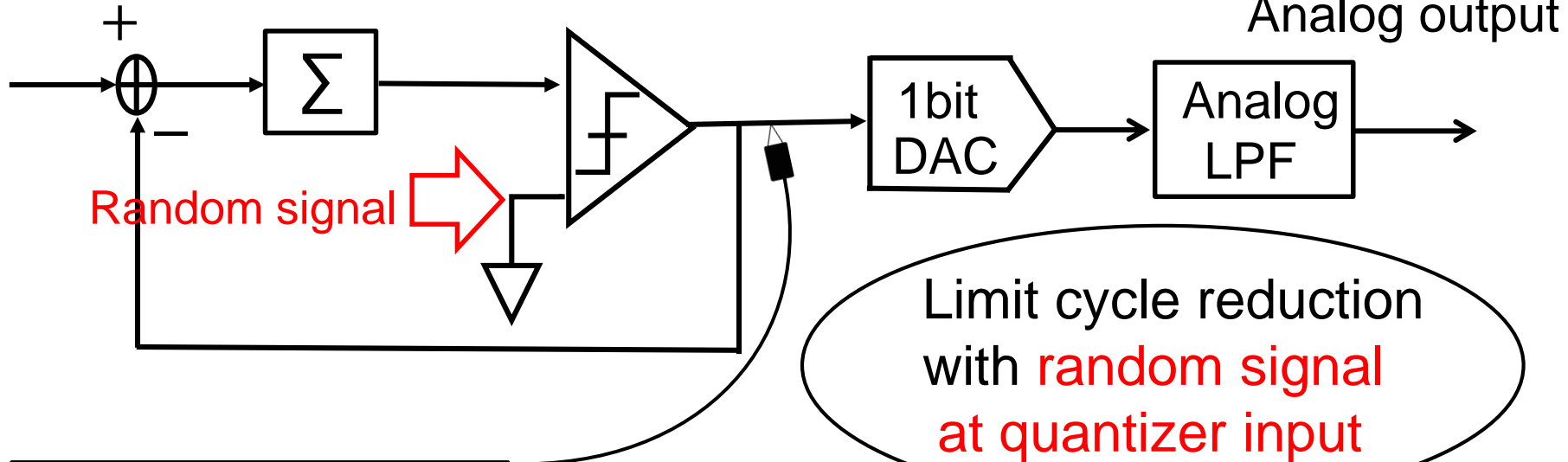


- Objective
- Limit cycle suppression
  - Relax LPF requirement



# Our Studies

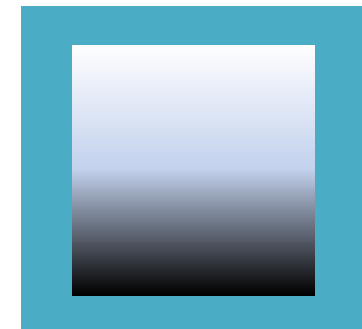
Digital input



Limit cycle

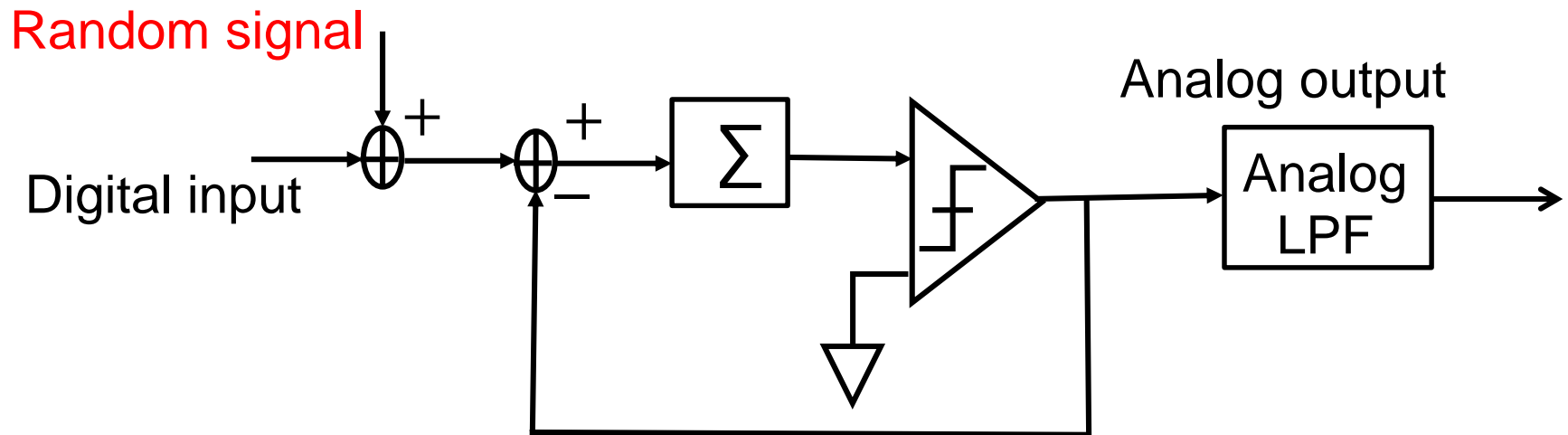


Stair



Smoothness !

Adding random signal to digital input



## Drawbacks

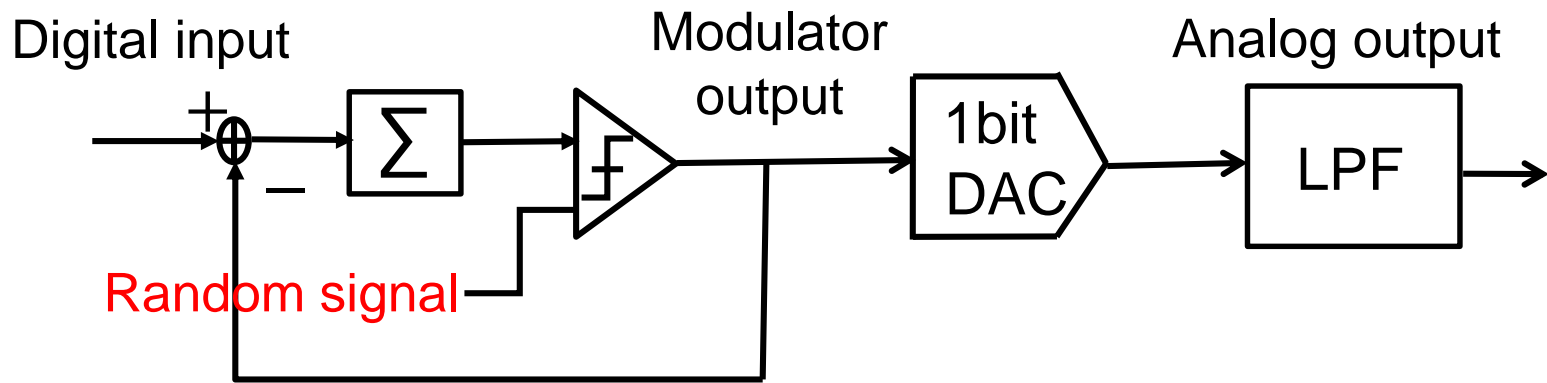
- Input range sacrifice
- Random signal has to be out of signal band

➡ difficult to generate

- Research Background
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# Proposed Method

12/24



## < Features >

- ① NOT sacrifice input range
- ② NOT affect signal band, thanks to noise-shaping
- ③ Easily generate random signal.

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# Simulation Configuration

◆ In 10-bit case

Digital dither signal

Random signal

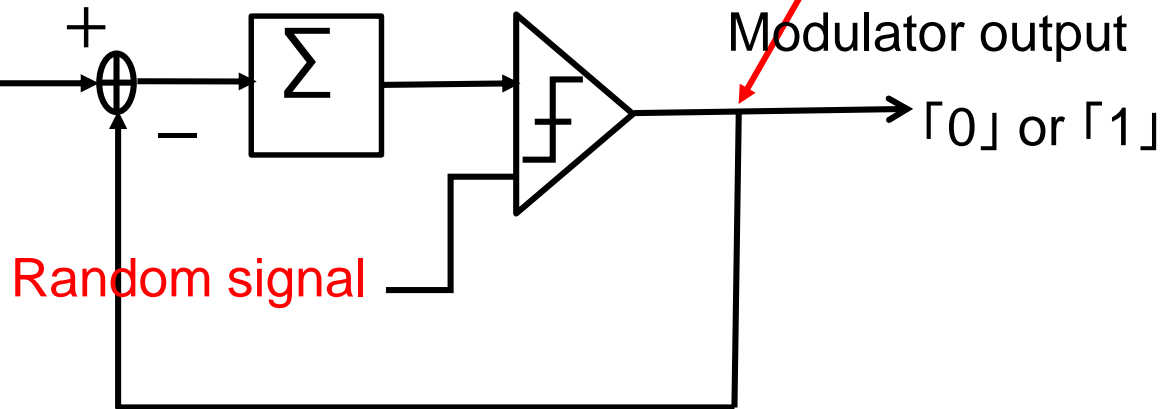
➔ Controlled by number of 1's

Random signal:

-1.0~+1.0, -2.0~+2.0, -3.0~+3.0

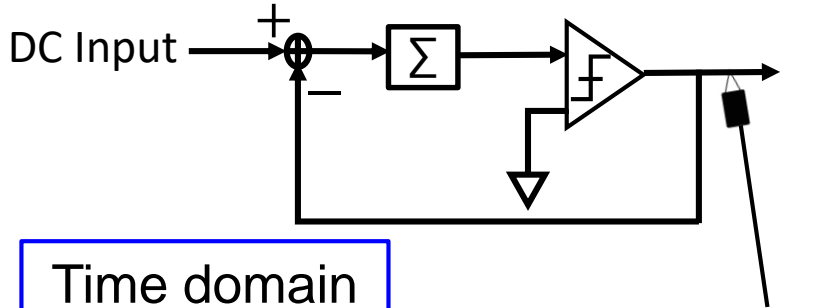
Digital signal

DC: -1.0~+1.0

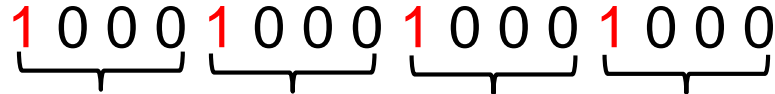


# Modulator Operation with Random Signal

- Without random signal

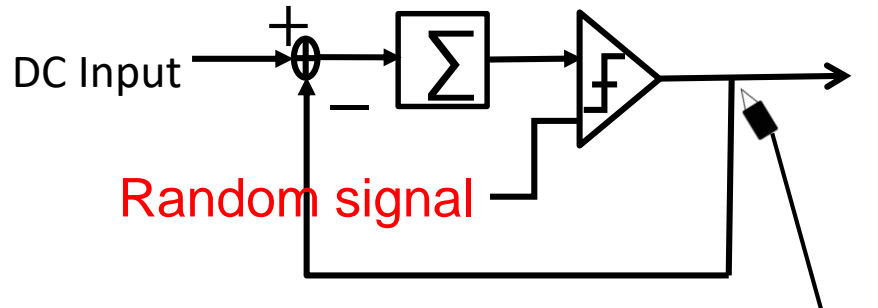


Time domain

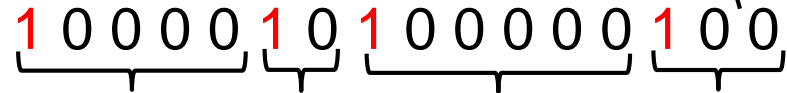


Period

- With random signal



Random signal



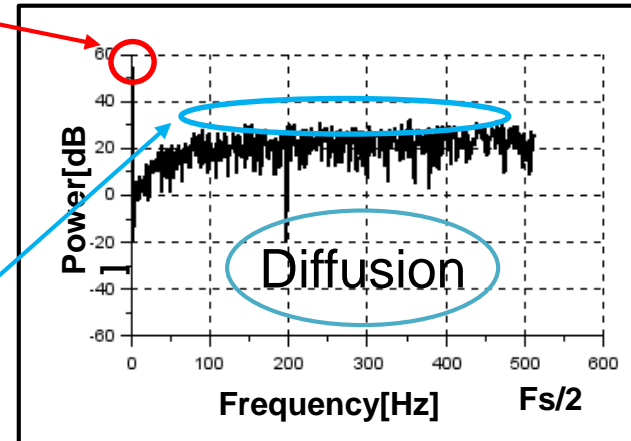
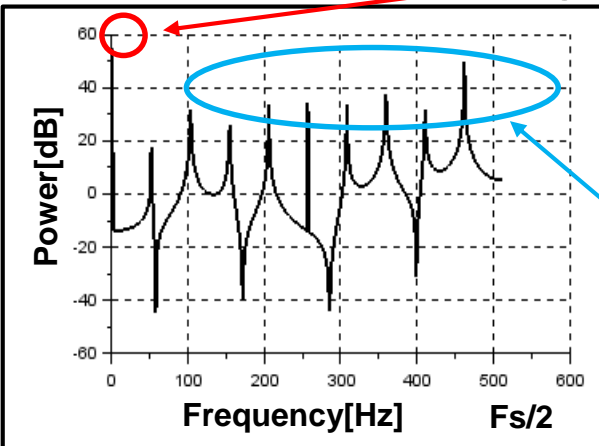
Not Periodic

✓ Orders of '0' and '1' ⇒ different

✓ Total numbers of 1's ⇒ the same

Frequency domain

DC signal power ⇒ the same



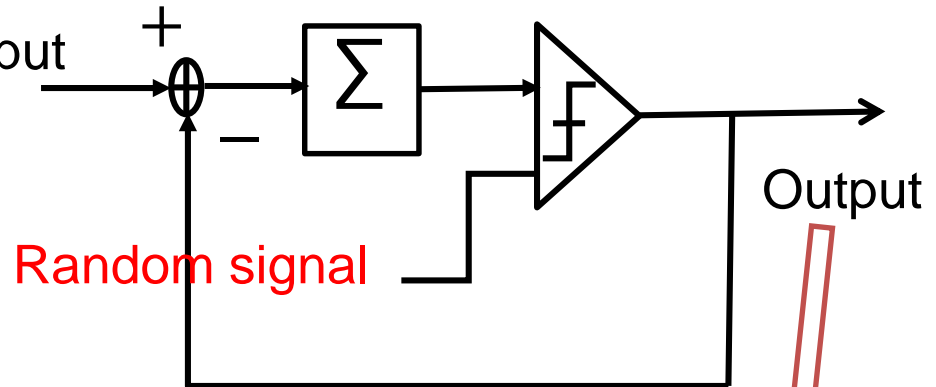
Linear

Noise

Diffusion

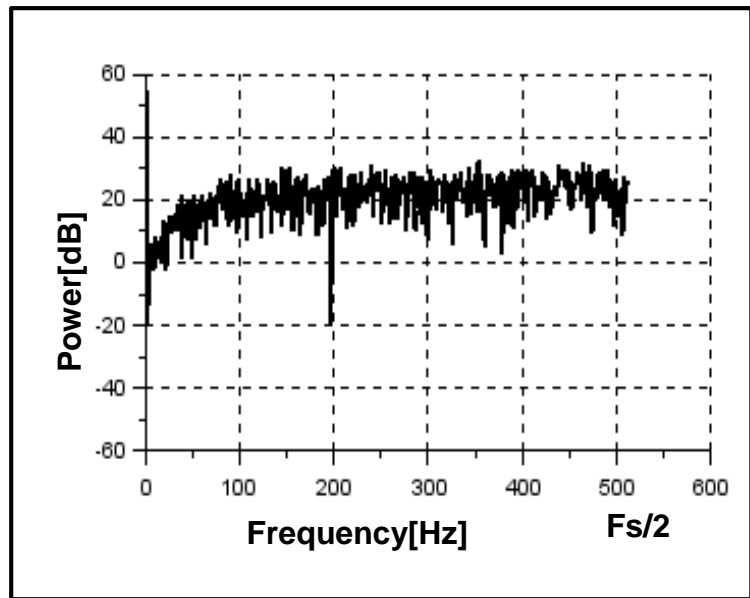
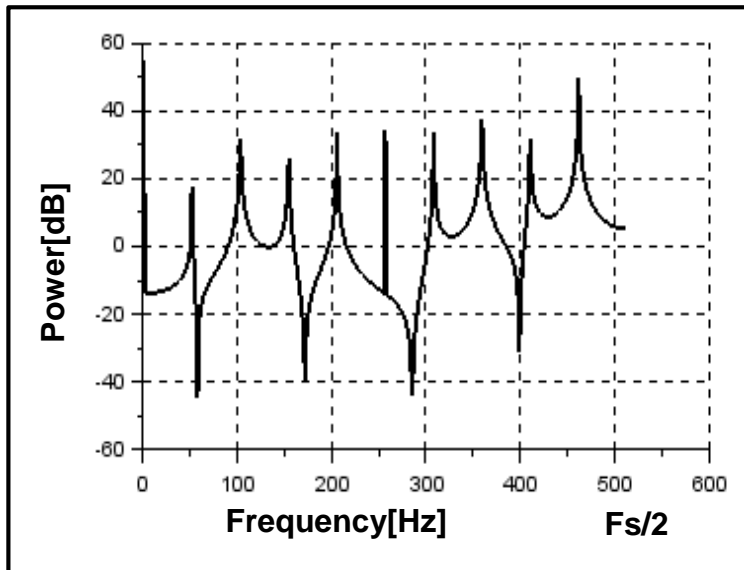
Random signal: -2.0 ~ +2.0

DC Input = 0.1



Without dither

Proposed





# SFDR (Spurious Free Dynamic Range)

10-bit first-order

LP case

DC = 0.1

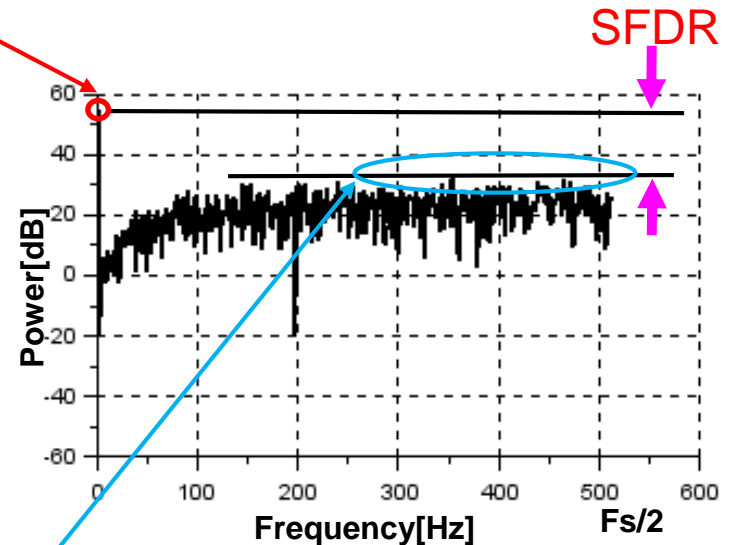
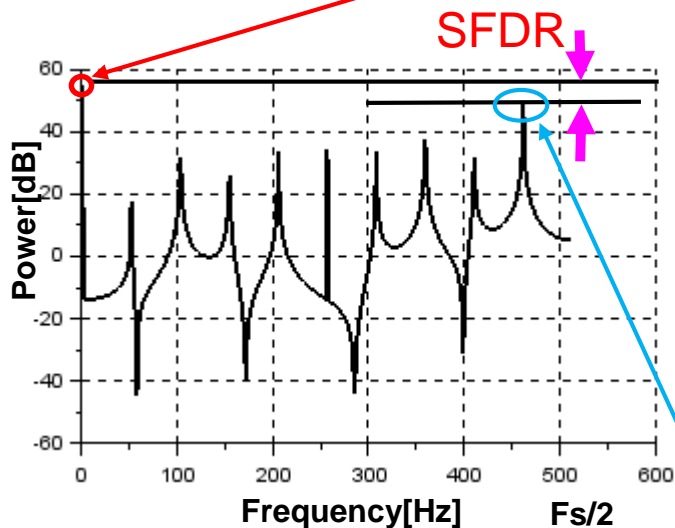
$$\text{SFDR} = \frac{\text{Signal Power}}{\text{Maximum Harmonics Power}}$$

$$\text{SFDR} = 5.39 \text{ dB} < 15.59 \text{ dB}$$

Without dither

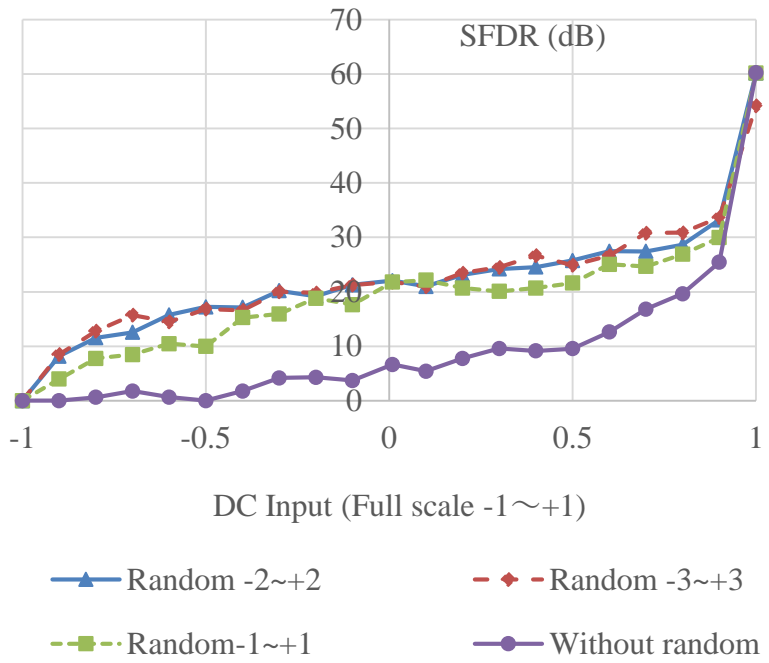
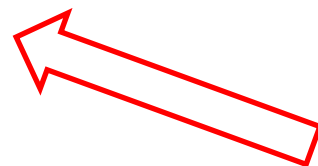
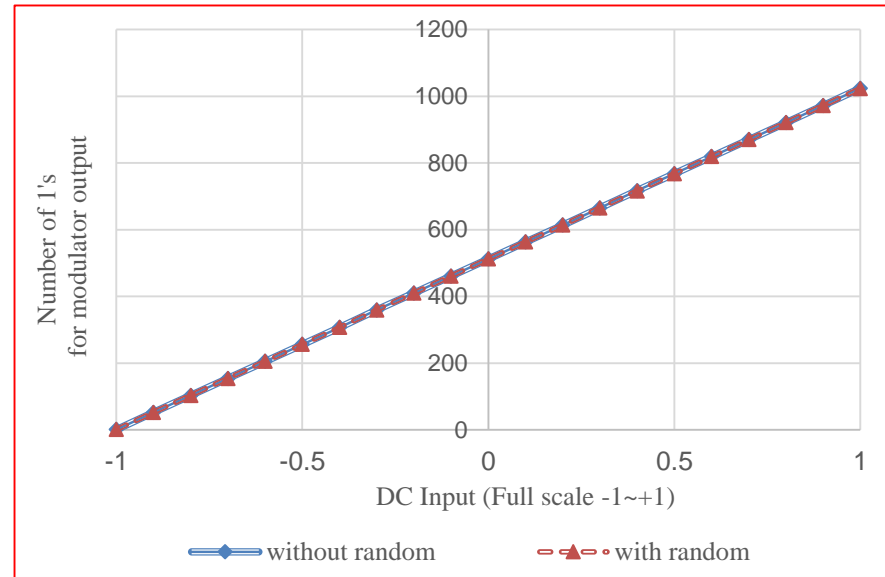
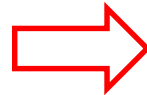
Signal Power

Proposed



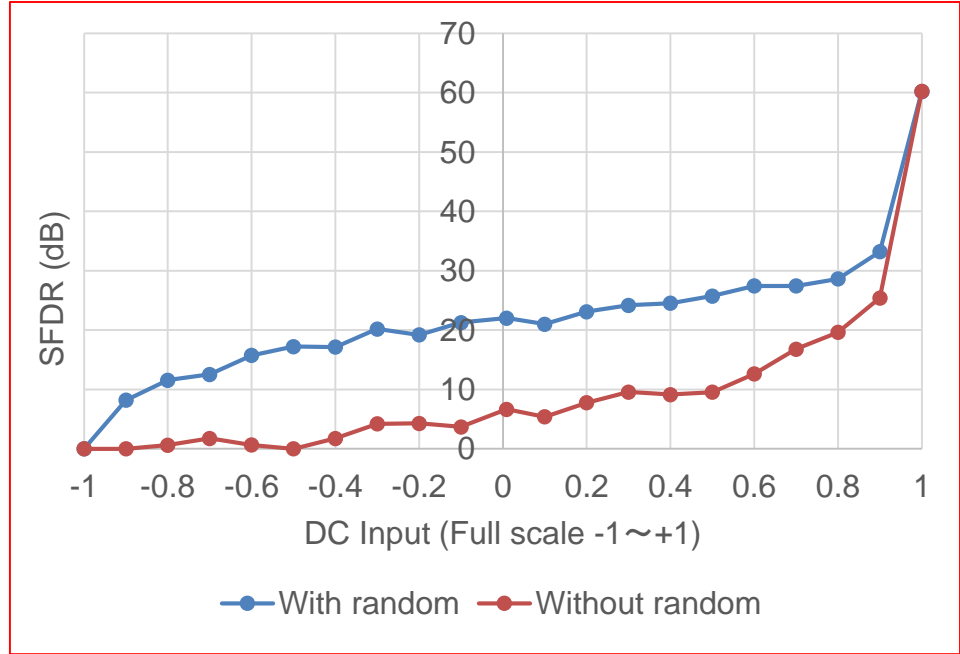
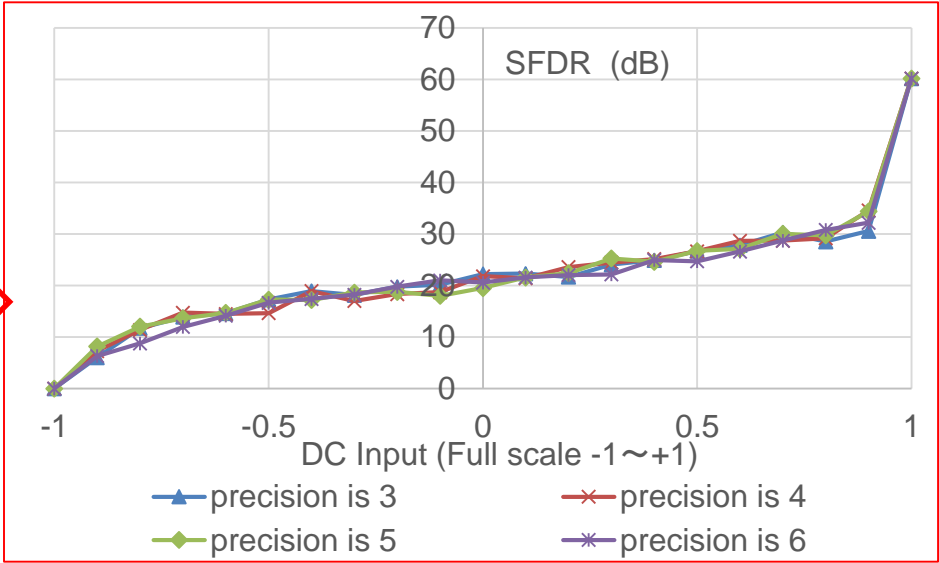
Maximum Harmonics Power

Linearity is confirmed with simulation result.

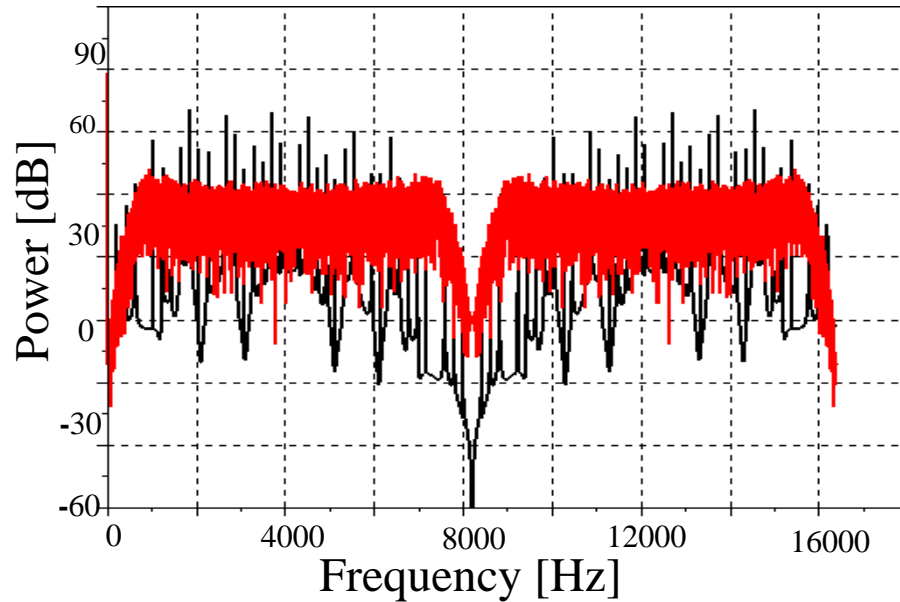


Ideal result can be obtained with random signal between -2.0 ~ +2.0

“precision 3” → 1.782  
“precision 4” → 1.7824  
“precision 5” → 1.78245



SFDR → much improved

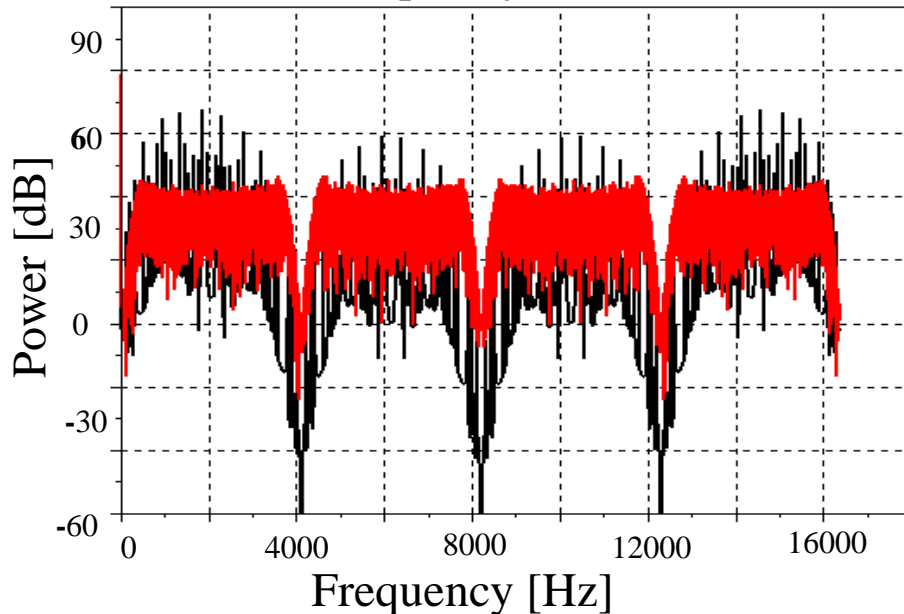


2-band BP modulator

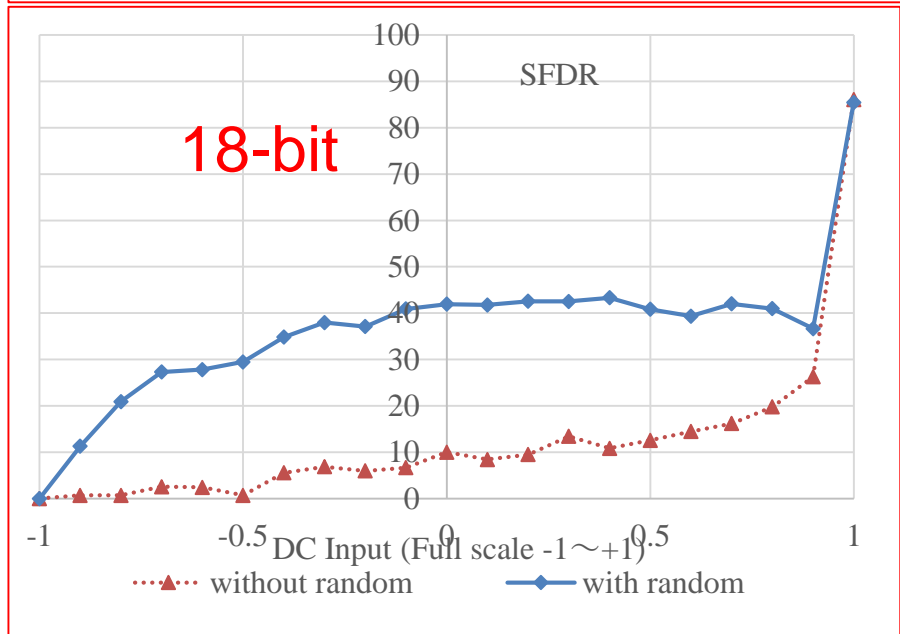
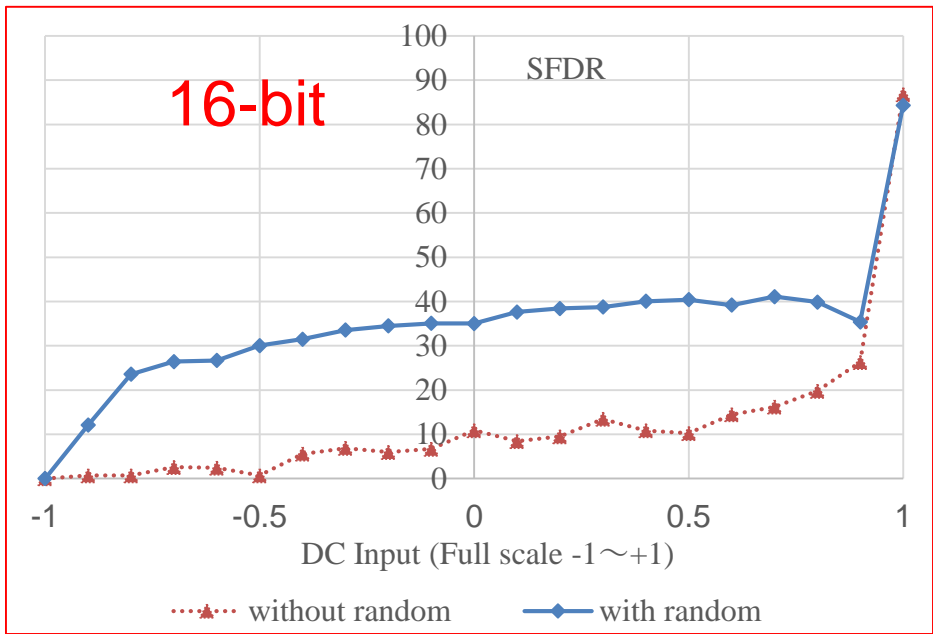
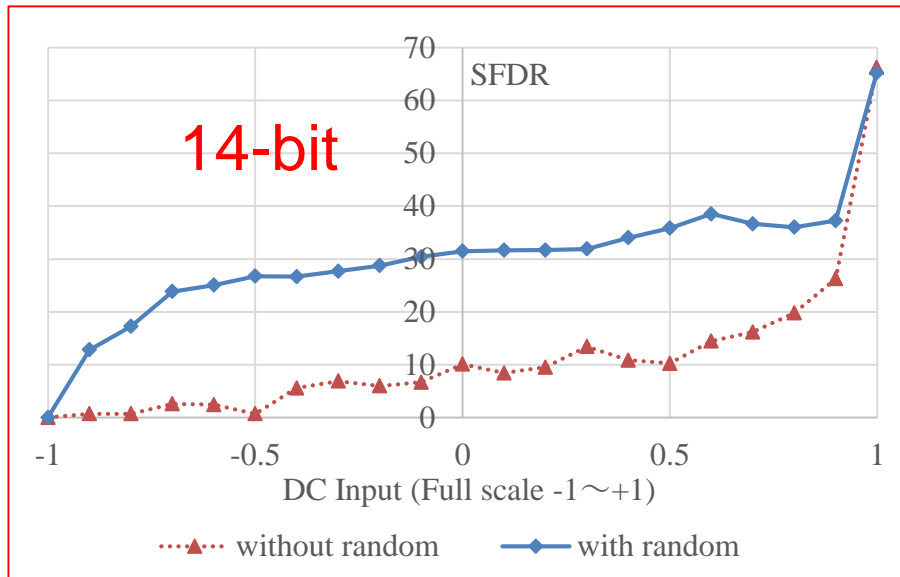
Red → Spectrum with random signal.

Black → Spectrum without random signal.

4-band BP modulator



Red line →  
without random  
signal.  
Blue line →  
with random signal.



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# Conclusion





<  $\Delta\Sigma$  DA modulator >

Conventional: Limit cycle problem for small input



Proposed: Using random signal at quantizer input



- Limit cycle  reduced
- SFDR much  improved
- Overall linearity of  $\Delta\Sigma$  DA modulator  maintained.
- Above statements  valid for all LP, HP, BP, multi-BP type modulators.

# Thanks for listening !

